MRI Brain Images Segmentation Based on Optimized Fuzzy Logic and Spatial Information

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Abstract— In this paper, a modified fuzzy c-means (FCM) clustering for medical image segmentation is presented. A conventional FCM algorithm does not fully utilize the spatial information in the image. In this research, we use a FCM algorithm that incorporates spatial information into the membership function for clustering. The spatial function is the summation of the membership function in the neighborhood of each pixel under consideration. The advantages of the method are that it is less sensitive to noise than other techniques, and it yields regions more homogeneous than those of other methods. This technique is a powerful method for noisy image segmentation. Originality of this research is the methods applied on a normal MRI brain image and a glioma MRI brain images, and analyze the area of tumor from segmented image. The results show that the method effectively segmented Magnetic Resonance Imaging (MRI) brain images with spatial information, and the segmented normal and glioma MRI brain images can be analyzed for diagnosis purpose. And, the area of abnormal mass is identified from 9.65 to 27.71 cm².

Index Term— Adaptive image segmentation, fuzzy logic, FCM clustering, MRI brain image, spatial information

I. INTRODUCTION
Image segmentation is a challenging task in image analysis. To satisfy increasing requirement of image segmentation, a variety of segmentation methods have been developed over past several years. FCM (Fuzzy c-means) is an unsupervised technique that has been successfully applied to future analysis, clustering, and classifier designs in the fields such as astronomy, geology, medical imaging, target recognition, and image segmentation. An image can be represented in various feature spaces, and the FCM method classifies the image by grouping similar data points in the feature space into clusters.

There has been considerable interest recently in the use of fuzzy segmentation methods, which retain more information from the original image than hard segmentation methods (e.g., Bezdek et al. [1], Udupa et al. [2], Pham [3]). The fuzzy C-means method (FCM), in particular, can be used to obtain a segmentation via fuzzy pixel classification. Unlike hard classification methods which force pixels to belong exclusively to one class, FCM allows pixels to belong to multiple classes with varying degrees of membership. This approach allows additional flexibility in many applications and has recently been used in processing of magnetic resonance image (MRI) [4]. For example, in their segmentation of MRI brain images, Pham et al. [5] thresholded the FCM memberships in order to extract pixels which have a high confidence of correct classification. Xu et al. [6] used deformable surfaces that converged to the peaks of the memberships. The FCM method, however, does not address the intensity inhomogeneity artifact that occurs in nearly all MRI [7]-[8]. Originality of this research is the method applied on a normal MRI brain image and a glioma MRI brain images, and analyze the area of tumor from segmented images.

II. FUNDAMENTAL THEORY

A. Magnetic Resonance Imaging
In this section, we give a brief description of the principles of Magnetic Resonance Imaging (MRI) which are referred to [9]. MRI is an imaging technique used primarily in medical settings to produce high quality images of the inside of the human body. In MRI, the image is a map of the local transverse magnetization of the hydrogen nuclei. This transverse magnetization in turn depends on several intrinsic properties of the tissue. The magnetic resonance phenomenon relies on the fundamental property that protons and neutrons that make up a nucleus possess an intrinsic angular momentum called spin. When protons and neutrons combine to form nucleus, they combine with oppositely oriented spins. Thus, nuclei with an even number of protons and neutrons have no net spin, whereas nuclei with an odd number of protons or neutrons possess a net spin. Hydrogen nuclei have an signal since its nucleus is made up of only a single proton and possess a net spin. The human body is primarily fat and water, which have many hydrogen atoms. Medical MRI primarily images the magnetic resonance signal from the hydrogen nuclei in the body tissues.

The net spin of the nucleus around its axis gives it an angular moment. Since the proton is a positive charge, a current loop perpendicular to the rotation axis is also created, and as a result the proton generates a magnetic field. The joint effect of the angular moment and the self generated magnetic field gives the proton a magnetic dipole moment parallel to the rotation axis. Under normal condition, one will not experience any net magnetic field from the volume since the magnetic dipole moments are oriented randomly and on average equalize one another.

When placed in a magnetic field, a proton with its
magnetic dipole moment processes around the field axis. The frequency of this precession, \( \nu_0 \), is the resonant frequency and is called the Larmor frequency. The precession frequency is directly proportional to the strength of the magnetic field, i.e.

\[
v_0 = gB_0
\]

where \( B_0 \) is the main magnetic field strength, and \( g \) is a constant called gyromagnetic ratio which is different for each nucleus (42.56 MHz/Tesla for protons).

Given a specimen, the application of a magnetic field \( B_0 \) would create a net equilibrium magnetization \( M_0 \) per cubic centimeter, which is aligned to the \( B_0 \) field. The \( M_0 \) is the net result of summing up the magnetic fields due to each of the \( H \) nuclei and is directly proportional to the local proton density (or spin density). However, \( M_0 \) is many orders of magnitude weaker than \( B_0 \) and is not directly observable. By tipping \( M_0 \) away from the \( B_0 \) field axis with an appropriate RF pulse having a frequency equals to the Larmor frequency, a longitudinal magnetization component ML and a transverse magnetization component MT is produced. When the RF pulse is turned off, the longitudinal magnetization component ML recovers to \( M_0 \) with a constant required for the FID response signal from a given tissue type to decay. The FID response signal is measured by an RF coil placed around the object being imaged.

When MRI images are acquired, the RF pulse is repeated at a predetermined rate. The period of the RF pulse sequence is the repetition time, TR. The FID response signals can be measured at various times within the TR interval. The time between which the RF pulse is applied and the response signal is measured is the echo delay time, TE. The TE is the time when the spin echo occurs due to the refocusing effects of the 180 degree refocusing pulse applied after a delay of TE/2 from the RF pulse. The TR and TE control how strongly the local tissue relaxation times, T1 and T2, affect the signal. By adjusting TR and TE the acquired MR image can be made to contrast different tissue types.

### B. Image Segmentation

Much past work on medical image segmentation relied strictly on human graphical interaction to define regions, using methods such as manual slice editing, region painting and interactive thresholding. Rajapakse [10] classified the different methods of image segmentation as four main categories. (1) The classical methods such as thresholding region growing and edge based techniques. (2) The statistical methods such as the maximum-likelihood classifier (MLC). These methods are basically supervised and depend on the prior model and its parameters. Vannier et al. [11] reported satisfactory preliminary results with Bayesian MLC. Ozkan et al. [12] made a comparison between the MLC and the neural network classifier which showed the superiority of the neural network. New methods of segmentation that could be classified as statistical methods have been introduced in the past few years. Hansen [13] used a probabilistic supervised relaxation technique for segmenting 3D medical images. The method introduced the use of cues to guide the segmentation. Those cues marked by the user have the mean and standard deviation as description parameters. (3) The neural networks methods one example of which is the work of Ahmed et al. [14] who used a two stages neural network system for CT/MRI image segmentation. The first stage is a self-organized principal component analysis (SOPCA) network and the second stage consists of a self-organizing feature map (SOFM). The results obtained compare favorably with the classical and statistical methods. (4) The Fuzzy Clustering methods. In [15] a comparison between the fuzzy clustering and neural network techniques in segmenting magnetic resonance images of the brain debated for the need of unsupervised technique in segmentation which was provided using the unsupervised fuzzy c-mean algorithm. However the long time taken by the fuzzy c-mean algorithm was documented.

### III. FUZZY C-MEANS CLUSTERING

The FCM algorithm assigns pixels to each category by using fuzzy memberships. Let \( X=(x_1, x_2, \ldots, x_N) \) denotes an image with \( N \) pixels to be partitioned into \( c \) clusters, where \( x_i \) represents multispectral (features) data. The algorithm is an iterative optimization that minimizes the cost function defined as follows [16]:

\[
J = \sum_{j=1}^{N} \sum_{i=1}^{c} u_{ij}^m \| x_j - v_i \|^2
\]

where \( u_{ij} \) represents the membership function of pixel \( x_j \) in the \( i \)th cluster, \( v_i \) is the \( i \)th cluster center, and \( m \) is a constant. The parameter \( m \) controls the fuzziness of the resulting partition, and \( m = 2 \) is used in this study.

The cost function is minimized when pixel close to the centroid of their clusters are assigned high membership values, and low membership values are assigned to pixels with data far from the centroid. The membership function represents the probability that a pixel belongs to a specific cluster. In the FCM algorithm, the probability is dependent solely on the distance between the pixel and each individual cluster center in the feature domain. The membership functions and cluster centers are updated by the following:

\[
u_{ij} = \frac{1}{\sum_{k=1}^{c} \left( \frac{\| x_j - v_i \|}{\| x_j - v_k \|} \right)^{2/(m-1)}}
\]
\[
V_i = \frac{\sum_{j=1}^{N} u_{ij}^m x_j}{\sum_{j=1}^{N} u_{ij}^m}
\]

where \(u_{ij} \in [0, 1]\).

Starting with an initial guess for each cluster center, the FCM converges to a solution for \(v_i\), representing the local minimum or a saddle point of the cost function. Convergence can be detected by comparing the changes in the membership function or the cluster center at two successive iteration steps.

One of the important characteristics of an image is that neighboring pixels possess similar feature values, and the probability that they belong to the same cluster is great. This spatial relationship is important in clustering, but it is not utilized in a standard FCM algorithm. To exploit the spatial information, a spatial function is defined as:

\[
h_{ij} = \sum_{k \in \text{NB}(x_j)} u_{ik}
\]

where \(\text{NB}(x_j)\) represents a square window centered on pixel \(x_j\) in the spatial domain. A \(3 \times 3\) window was used throughout this work. Just like the membership function, the spatial function \(h_{ij}\) represents the probability that pixel \(x_j\) belongs to \(i\)th cluster. The spatial function of a pixel for a cluster is large if the majority of its neighborhood belongs to the same cluster. The spatial function in incorporated into membership function as follows:

\[
u_{ij} = \frac{u_{ij}^p h_{ij}^q}{\sum_{k=1}^{N} u_{ik}^p h_{ik}^q}
\]

where \(p\) and \(q\) are parameters to control the relative importance of both functions. In a homogenous region, the spatial functions fortify the original membership, and the clustering result remains unchanged. However, for a noisy pixel, this formula reduces the weighting of a noisy cluster by the labels of its neighboring pixels. As a result, misclassified pixels from noisy regions or spurious blobs can easily be corrected. The spatial FCM with parameter \(p=1\) and \(q=2\) is identical to the conventional FCM.

The clustering is a two-pass process at each iteration. The first pass is the same as that in standard FCM to calculate the membership function in the spectral domain. In the second pass, the membership information of each pixel is mapped to the spatial domain, and the spatial function is computed from that. The FCM iteration proceeds with the new membership that is incorporated with the spatial function. The iteration is stopped when the maximum difference between two cluster centers at two successive iterations is less than a threshold \((\varepsilon=0.02)\). After the convergence, defuzzification is applied to assign each pixel to a specific cluster for which the membership is maximal.

IV. EXPERIMENTAL RESULTS

A. Normal MRI Brain Image

In this research, MRI image is segmented using FCMS method incorporated into the spatial information. Fig. 1 shows the 256x256 grayscale original MRI1 brain image. Fig. 1(a) and (b) show the T1- and T2-weighted MRI1 images, respectively. Fig. 2(a) and (b) show the results of the FCM incorporated into the spatial information with parameters \(p=1\) and \(q=2\).

![Fig. 1. Original normal MRI1 brain images: (a) T1-weighted MRI1 image and (b) T2-weighted MRI1 image.](image)

As can be seen in the segmented images in Fig. 2, lesion or abnormal mass is not identified, and the ventricular system is not extensive and it is a median. So, the image is a normal brain MRI image.

Fig. 3(a) to (f) show the 256x256 original MRI brain images with tumor used for this study [17], while Fig. 4(a) to (f) demonstrate the results of segmentation of each images from Fig. 3. Fig. 3(a) shows an original axial proton density image of MRI2 demonstrating the lesion as solid, with a high signal, while Fig. 4(a) shows the result of segmentation of the image. Fig. 3(b) and Fig. 4(b), MRI3, show the tumor arising in the pons. The fourth ventricle is displaced and slightly enlarged. Fig. 3(c), a noncontrast, T2-weighted axial image of MRI4, demonstrates the presence of the tumor and the increased signal on T2 weighting of the CSF-filled, resected space. The three planes allow excellent delineation of the residual tumor versus the tumor volume that has been resected. They also allow evaluation of the area of postsurgical charge and disruption of the blood-brain barrier in an area where the tumor has been resected and shows characteristic enhancement.
Fig. 2. Segmented Normal MRI Brain images: (a) Segmented T1-weighted MRI image and (b) Segmented T2-weighted MRI image.

Fig. 3. Original MRI brain images with tumor: (a) MRI2, (b) MRI3, (c) MRI4, (d) MRI5, (e) MRI6, (f) MRI7.

Fig. 4. (a) Segmented MRI2, (b) segmented MRI3, (c) segmented MRI4, (d) segmented MRI5, (e) segmented MRI6, (f) segmented MRI7.

Fig. 3(d) is an axial image of MRI5 demonstrating the tumor. The extent of the tumor can be appreciated by its sharp contrast to the normal surrounding tissue. The ventricular distortion can also be appreciated. Fig. 3(e), MRI6, show tumor involving the thalamic and basal ganglia region of the right. The delineation of the tumor involvement and the normal surrounding brain tissue is very easily done, and there is good tumor demaraction. Fig. 3(f), MRI7, demonstrates a large left frontoparietal tumor. The size and surrounding edema are fairly marked. There is also evidence of spread into the midline body of the corpus callosum.

B. Analysis of the Area of Tumor

In this study, we also apply the FCM method to segment six 256x256 MRI brain images with tumor (i.e. MRI2, MRI3, MRI4, MRI5, MRI6, and MRI7), as shown in Fig. 3 [17]. Application of the FCMS method in segmentation of the images is in order to analysis of the area of tumor. Fig. 4 shows the 256x256 segmented MRI2 to MRI7 images, respectively.

Table I shows the area of abnormal mass of segmented MRI images. The results are MRI images identified tumors of 9.65 to 27.71 cm$^2$ or 3.59 to 10.31% of the areas in percentage. In the brain tumor, a glioma, the bigger area of a tumor the higher grade of a glioma.
Table II shows the results of misclassification of segmentation of MRI brain images with tumor using K-means, FCM, and FCMS methods, respectively. The results show that FCMS method is better than K-means and FCM methods in classification of segmentation.

V. CONCLUSIONS

In this research, we use FCMS method that incorporates the spatial information into the membership function to improve the segmentation results. The membership functions of the neighbors centered on a pixel in the spatial domain are enumerated to obtain the cluster distribution statistics. These statistics are transformed into a weighting function and incorporated into the membership function. This neighboring effect reduces the number of spurious blobs and biases the solution toward piecewise homogeneous labeling. The method use to analyze normal MRI brain and glioma MRI brain images. We applied the technique on a normal MRI brain image and on a glioma MRI brain image. The results show that the method effectively segmented MRI brain images with spatial information, and the segmented normal and glioma MRI brain images can be analyzed for diagnosis purpose. And, the area of abnormal mass is identified from 9.65 to 27.71 cm². Our results using FCMS method are more accurate than K-means and FCM methods in classification of segmentation. Finally, we suggest to the readers that the application of the FCMS method to other abnormal brain cases will be the topic for further research.

REFERENCES


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